Experimental Demonstration of an Electrostatic Orbital Angular Momentum Sorter for Electron Beams

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The component of orbital angular momentum (OAM) in the propagation direction is one of the fundamental quantities of an electron wave function that describes its rotational symmetry and spatial chirality. Here, we demonstrate experimentally an electrostatic sorter that can be used to analyze the OAM states of electron beams in a transmission electron microscope. The device achieves postselection or sorting of OAM states after electron-material interactions, thereby allowing the study of new material properties such as the magnetic states of atoms. The required electron-optical configuration is achieved by using microelectromechanical systems technology and focused ion beam milling to control the electron phase electrostatically with a lateral resolution of 50 nm. An OAM resolution of $1.5\hbar$ is realized in tests on controlled electron vortex beams, with the perspective of reaching an optimal OAM resolution of $1\hbar$ in the near future.

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Although electron microscopy was pioneered in the early 1930s [1], the discipline continues to be developed technically and methodologically [2,3]. A modern transmission electron microscope can be used to characterize materials with sub-0.1-nm spatial resolution [4–6], to provide three-dimensional microstructural and compositional information [7], to record electron energy-loss spectra with a sensitivity of a few meV [8,9], and to achieve new horizons in protein characterization [10,11]. One of the most significant advances has been the theoretical and experimental development of spherical aberration correction [12–14], which requires the precise manufacture, alignment, and control of the magnetic fields of electron-optical elements using computer-aided procedures and electronics. Recently, other concepts have been taken from light optics and used to explore new directions in electron-optical instrumentation.

For example, synthetic holograms have been used to realize electron vortex beams [15–24], nondiffractive beams [25,26], and new measurement schemes [27–29]. These developments have been used to introduce the component of orbital angular momentum (OAM) in the propagation direction (henceforth defined $z$) as a “new” degree of freedom in electron microscopy. However, the use of synthetic holograms is detrimental to electron beam coherence and intensity, motivating the use of electrostatic and magnetostatic fields to achieve electron beam control [30–32].

Here, we realize an electrostatic “sorter” for electrons that can be used to measure the OAM components of an electron beam. The $z$ component of the OAM operator is proportional to the gradient of the electron wave function with respect to the azimuthal coordinate $\theta$, according to the expression $L_z = -i\hbar \partial_\theta$. Its eigenstates are electron vortex beams, which are characterized by azimuthal phase terms and can be described in the form $e^{-i l \theta}$. The measurement of an OAM state is therefore equivalent to finding the value of $l$. We realized such a device based on two holographic phase elements fabricated from SiN [27]. In the present study, we demonstrate a complete setup that is based on the
use of controllable electrostatic fields and can be retrofitted to an existing electron microscope.

An OAM sorter is intended to study an electron beam after its interaction with a sample [33–35]. Previous work focused on postselection of linear momentum after elastic and, more interestingly, inelastic scattering of electron beams [36,37]. However, little has been achieved in terms of control of the OAM final state. Electron energy-loss spectroscopy with OAM postselection could be used to assess magnetic dichroism [33–35], to discriminate multipolar transitions [38], to study two-dimensional materials [39], and for more exotic applications [40]. However, efficient and accurate measurement is required for this to become a valuable tool in materials science and cryoelectron microscopy [41].

Previous methods of OAM measurement [42–49] were based on diffraction by components such as amplitude apertures. In contrast, an OAM sorter provides decomposition of all OAM channels at the same time by making use of a conformal mapping from Cartesian to log-polar coordinates. Such a coordinate transformation permits radial and azimuthal degrees of freedom to be decoupled. Since it corresponds to a unitary change of basis, all of the components of the electron beam that have a chosen OAM value are propagated into a single region of space with virtually no loss and with superior efficiency to the use of a pitchfork hologram [50], despite the simplicity of the latter concept. Although the Stern-Gerlach-like approach described in Ref. [47] also offers a potentially near-unitary transformation, it does not decouple radial and azimuthal degrees of freedom.

Here, we describe the technical steps that are required to realize an electrostatic OAM sorter. We present preliminary results that demonstrate its successful operation, including the recording of OAM spectra in a transmission electron microscope.

Whereas an OAM sorter that is based on the use of synthetic holograms follows an equivalent light-optical holographic approach [51], McMorran et al. showed theoretically [30] that a set of electrodes is able to reproduce the required phase elements. This proposal was improved by Pozzi et al. [31], who proposed the use of additional electrodes outside the area of the beam. In addition, it was realized that all conformal mappings can be reproduced by the use of near-harmonic phase elements, such as those produced by electrodes [52]. Conformal mappings in optics involve transformations of coordinates by imparting appropriate phase gradients (and therefore in-plane velocities) to wave functions and allowing them to evolve to corresponding diffraction planes. They can be achieved by using two phase elements and making use of quantum mechanical changes of basis to measure quantities such as OAM. According to theory [30,31], a first sorter element $S_1$ (or “unwrapper”) can take the form of a long needle located in front of an electrostatic mirror. To a first approximation, such a needle can be modeled as a straight line of constant charge density or, equivalently, as an ellipsoid-shaped electrode that corresponds to a desired equipotential contour. An electrostatic mirror (i.e., a grounded flat electrode) should be positioned in front of the needle to ensure charge neutrality. The needle introduces a phase cusp, which unwraps the electron beam so that an azimuthal phase gradient is transformed into a linear gradient in the stationary phase approximation. This transformation is completed in the far-field diffraction plane, where a second phase element $S_2$ (or “sorter corrector”) removes the transformational phase and the beam can continue without rewrapping again. The second element can take the form of a series of in-plane parallel needle-shaped electrodes of alternating opposite polarity.

It is convenient to use complex notation to describe mappings from complex coordinates $u = x + iy$ to $u' = x' + iy'$, where $x$, $y$ and $x'$, $y'$ are orthogonal to the main propagation direction. The first conformal mapping can be expressed $u' = s f \ln(u/L)$, where $s$ is a transformation scale parameter (approximately equivalent to the average tilt imparted by element $S_1$). $f$ is the focal length of the lens system between the elements, and $L$ is a characteristic length (corresponding to the length of the needle in the electrostatic case). Element $S_1$ applies a phase distribution of the form

$$\phi_1 = \frac{s}{\lambda} \text{Re} \left\{ u \ln \left( \frac{u}{L} \right) - u \right\},$$  

while element $S_2$ applies a compensating phase distribution of the form

$$\phi_2 = \frac{Ls}{\lambda} \text{Re} \left\{ \exp \left( \frac{u}{s} \right) \right\},$$  

where $\text{Re}$ is the real value of a function and $\lambda$ is the electron wavelength. (See the Supplemental Material [53]).

Based on this initial design, we have developed devices that can be fitted into an electron microscope. Without altering the microscope significantly, i.e., without adding lenses, we realized OAM sorter elements $S_1$ and $S_2$ using apertures that were fabricated using microelectromechanical systems (MEMS) technology, one of which was placed in the back focal plane of the objective lens and the second in a selected area diffraction (SAD) plane. The aperture holders were custom-made and equipped with housings for $4 \times 11$ mm MEMS chips with sockets based on those used in a Thermo Fisher NanoEx-i/v specimen holder. MEMS fabrication involved two-dimensional patterning of the device electrodes using optical lithography and deep reactive ion etching of silicon-on-insulator wafers using a recessed etching isolation technique. Up to 8 electrical pins could be used inside the microscope by connecting the internal to the external sockets through the body of each aperture holder. The use of MEMS technology in a planar geometry in a restricted space required several changes from
the theoretical geometry. Needle $S_1$ was replaced by three needles, as recently reported calculations [31] showed that astigmatism introduced by a finite needle can be compensated by the use of lateral electrodes oriented perpendicular to it. The shapes of the needles were initially defined using MEMS fabrication and then adjusted to achieve more precise (on a 50 nm scale) ellipsoidal shapes using focused ion beam milling. A virtually infinite series of electrodes in device $S_2$ was approximated by 11 electrodes. Smart use of a planar topology with links behind the connection pads permitted the even pins to be connected to each other, while the odd pins could be driven independently. Figure 1 shows off-axis electron holography measurements of electrically biased MEMS chips inserted in the specimen plane of a standard Thermo Fisher NanoEx-i/v holder, confirming the expected phase distributions. The phase profile for $S_1$ is almost ideal. The $S_2$ phase contours are also almost ideal, in particular close to the central pins. Although the influence of truncation resulting from the use of only 11 needles is visible, it does not affect the region of the central 5 electrodes significantly. Figure 2(a) shows a schematic diagram of the positions of the phase elements and their effect on the electron beam. Experiments were performed at 300 kV in a Thermo Fisher Titan G2 60-300 transmission electron microscope, which is equipped with an X-FEG electron emitter and an image spherical aberration corrector. The illumination system was set to spot size 9 and the three condenser lens system of the microscope was used to achieve a probe convergence semiangle of 2 mrad in the specimen plane. Although a specimen can be located in a standard position in the objective lens, for test purposes a synthetic hologram, which is referred to here as a “generation” hologram, was placed in the second condenser aperture plane, in order to generate a known electron beam (typically a superposition of vortex beams). The microscope was operated in “microprobe” mode, with the objective lens excited to a standard preset value. The lenses and multipoles in the image aberration corrector were switched off, in order to achieve a larger focal distance between the sorting
elements. In this configuration, the second sorter element \( S_2 \) was located in the diffraction plane of the first sorter element \( S_1 \) (mounted in the objective aperture plane), which is conjugate to the specimen plane. An OAM spectrum could then be recorded on the detector with the microscope set to diffraction mode. This microscope has two SAD planes (SAD1 and SAD2). In the present study, the upper (SAD1) plane was used.

The device was tested by using generation holograms in the condenser aperture plane to create electron beams with known OAM states \([27]\). The generation holograms were nanopatterned SiN membranes, in which thickness modulations were used to create intended phase distributions. With the image corrector unit turned off, an effective focal distance of \( f \approx 530 \) mm could be achieved. A voltage of \( V_c = -9.1 \) V applied to the main needle corresponded to a scale factor \( s \approx 3 \) \( \mu \)rad. The lateral needles of element \( S_1 \) were kept at \( V_L = -0.5 \) \( V_c \). For the \( S_2 \) element, the needles were biased with alternating voltages \( |V_{S_2}| = 16 \) V (with 8 V on the external ones). A change of applied bias could be compensated by a lateral shift of the beam. The alignment of the setup was found to be demanding, as the diffraction plane of element \( S_1 \) had to be matched in position, rotation, and magnification to element \( S_2 \). Under standard working conditions, a rotation angle of \( \sim 23^\circ \) was measured between the objective aperture and the SAD1 aperture. This angle was compensated by designing a rotated element \( S_2 \), with the residual rotation adjusted by applying a minor excitation to the adaptor and transfer lenses of the aberration corrector. The magnification introduced by element \( S_1 \) was adjusted by tuning the bias of the main \( S_1 \) needle (with the voltages of the lateral needles tuned accordingly). The position of the diffraction pattern on element \( S_2 \) was adjusted by using the image shift coils.

Figures 2(b)–2(d) show the evolution of an electron beam from a generation hologram mounted in the condenser aperture plane (reproduced almost exactly at the entrance of the \( S_1 \) element) to the diffraction plane of element \( S_1 \). The images show unwrapping of the vortex into Cartesian coordinates and finally an OAM spectrum. In Fig. 2(c), the logarithmic radial coordinate is on the horizontal axis, while the azimuthal coordinate is on the vertical axis. If element \( S_2 \) works perfectly, then the result is expected to comprise vertically separated peaks that describe the OAM spectrum of the beam. Slight bending is observed in practice, perhaps as a result of residual charging of the needle or imperfect centering of the needle on the optical axis.

Experimental spectra corresponding to different electron beam combinations are shown in Fig. 3 for synthetic
holograms with the indicated nominal OAM decompositions. A near-quantitative comparison with an independent evaluation (based on image analysis, as in Ref. [54]) of the OAM composition for a superposition of beams with \( l = \pm 5 \) is reported in the Supplemental Material, alongside secondary electron microscopy (SEM) images of generation holograms [53]. The experimental cross talk between different OAM channels is shown in Fig. 3(b) for input beams with values of \( \ell \) between 0 and 6. The values of cross talk depend on the specific details of each experiment.

The OAM resolution \( \Delta \ell \), which is defined here as the full width at half maximum of the spectrum, is found to be between 1.5 and 2, compared to an optimal value of unity [30]. This discrepancy is thought to result from imperfect alignment, while the background under each peak is likely to result from slight mismatch between the size of the diffraction pattern of element S1 and the size of element S2. The experimental OAM spectrum corresponding to a “standard” (azimuthally uniform) beam shown in Fig. 3(c) is reproduced nearly perfectly in the simulation shown in Fig. 3(d) by assuming a 1.1% error in the excitation of S1 and an 80 nm lateral misalignment between the two sorting elements. (See the Supplemental Material [53]). The figure also shows a comparison between experiment and simulation for the case of near complete correction. A more thorough comparison between simulations and experiments will be presented in a separate paper [55].

A standard beam obtained using a conventional condenser aperture should have an azimuthally uniform wave front. The beam that enters the sorter is almost exactly in a plane conjugate to that of the condenser aperture and should decompose to only an \( \ell = 0 \) component. The observed fringes result from misalignment. The absence of practically any material in the electron beam path (excluding the sorter 1 electrode) should rule out a spurious effect from the generation hologram. The simulations shown in Fig. 3(d) and an analytical model presented in the Supplemental Material [53] suggest that this mismatch is also responsible for the slight loss of resolution in the peaks. On the assumption that the phase mismatch is the primary limiting factor, two solutions can be proposed to improve the resolution.

(1) Since the phase mismatch is proportional to the phase gradient, the OAM resolution can be improved by reducing \( s \), i.e., the voltage applied to element S1, while maintaining the stationary phase condition \( (sR/\lambda) \gg \ell_{\text{max}} \) [31], where \( R \) is the size of the beam at the entrance of the sorter and \( \ell_{\text{max}} \) is the maximum value of OAM to be measured. If this approach is used, then the product \( sf \) must be matched to the periodicity of S2, which is fixed by the geometry of the S2 electrodes. For this reason, we increased the focal length by switching off the aberration corrector.

(2) In order to limit the phase gradient (and considering the geometric imperfection of sorter 1), it helps to limit the angle of acceptance of the sorter, for example, by using an aperture. In our tests without a sample, we simply reduced the convergence angle for this purpose.

Given the need for precise alignment, we believe that automatic diagnosis and alignment will be required regularly to reduce shift and magnification errors, in a manner similar to that used in adaptive optics in telescopes [56]. (See Ref. [57], and references therein).

In summary, we have described an OAM sorter for electron beams that is based on electrostatic phase elements and makes use of multiple-electrode-based control of electron wave functions. Experimental OAM spectra of test beams are found to be consistent with predictions. The OAM resolution is measured to be between \( \Delta \ell \approx 1.5 \) and 2. In the future, improved alignment using computer-based diagnostics is expected to provide an optimal resolution of \( \Delta \ell = 1 \) with a reduced background signal. The attainment of an ideal OAM resolution with the lossless efficiency of the electrostatic approach is expected to be important to achieve atomic-column-resolution magnetic measurements based on dichroism [58]. More generally, our demonstration of the use of MEMS-based technology to fabricate new components for charged particle optics offers a breakthrough for the measurement of previously inaccessible physical quantities, which are not limited to orbital angular momentum [52].

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