

**hilbert**

|                 |                   |          |  |
|-----------------|-------------------|----------|--|
| <b>keys:</b>    | <b>[from]</b>     | <number> | source picture   |
|                 | <b>[to]</b>       | <number> | output picture   |
| <b>options:</b> | <b>left/right</b> |          | transform vanishes over left/right half-plane  |
|                 | <b>zero</b>       |          | set imaginary part of central transform column to zero rather than duplicate real part |
|                 | <b>lp</b>         |          | apply low pass linear ramp filter to transform rows                                    |

The **hilbert** command calculates the discrete *hilbert* transform of a picture. It adds it as an imaginary part to the picture so that its *fourier* transform vanishes over one half-plane. You can use this operation to analyse images that are formed by one-sided imaging systems.

**Examples**

```
hilbert 1 2
```

This command copies the real part of picture 1 to *Complex* picture 2, and adds the row by row *hilbert* transform as an imaginary part. The *fourier* transform of picture 2 vanishes over the left half-plane.

```
hilbert right nozero
```

This command produces a picture whose *fourier* transform vanishes over the right half-plane, and whose imaginary row means match the real row means.

**Description**

The **hilbert** command adds a *hilbert* transform, as imaginary parts, row by row to the image, by suppressing one half of the row *fourier* transforms. You can specify the side using the **left/right** options, (by default the left side is used). The output is a *Complex* picture by default. The imaginary part of the row means (that is, of the central *fourier* component) are set to zero unless you specify option **nozero**, in which case the real part mean is copied across.

A *Hilbert* transformation is a convolution with  $\frac{1}{\pi x}$  and is like differentiation in the *x* direction, with a high-frequency de-emphasis. The convolution uses alternate points only of the source. Specifying the **lp** option causes an additional linear ramp filter to be included in the row transform manipulation, falling from 1 at the centre to zero at the outside. This filter approximates the convolution differently and weights all source points equally.

## hilbert

## Notes

multi-layer pictures: faulted  
 forms used internally: complex

## Defaults and Ranges

| keys/options | defaults  | range                |
|--------------|---|----------------------|
| [from]       | current picture, held in the variable <i>select</i> | valid picture number |
| [to]         | source picture                                      | valid picture number |
| left/right   | left  |                      |
| zero         | set to zero   |                      |